## Math 118 - Dr. Miller - Homework \#17: Triangle Properties

1. Is a triangle acute, right, or obtuse if its angle measures are...
(a) $30^{\circ}, 80^{\circ}$, and $x$
(b) $40^{\circ}, 50^{\circ}$, and $x$
(c) $20^{\circ}, 60^{\circ}$, and $x$
(d) $x, 2 x$, and $3 x$
(e) $x, x+2$, and $x+4$
2. Explain why a triangle cannot have both an obtuse and a right angle.
3. Find the measure of each angle of a triangle whose angles measure $x+67.25^{\circ}, 2 x-15.8^{\circ}$, and $x+10.15^{\circ}$.
4. The measure of one angle of a triangle is twice that of another angle. The third measures $68.4^{\circ}$. Find the measure of each angle of the triangle.
5. One angle of a triangle has a measure that is $12.8^{\circ}$ more than twice that of a second angle. The third angle has measure $17.4^{\circ}$ less than the second one. Find the measure of each angle.
6. Classify each statement as always true, sometimes true, or never true:
(a) A right triangle is isosceles.
(b) A right triangle is obtuse.
(c) An equilateral triangle is acute.
(d) A scalene triangle is acute.
(e) An obtuse triangle is scalene.
(f) A right triangle is equiangular.
7. (a) acute
(b) right
(c) obtuse
(d) right
(e) acute
8. A triangle having both an obtuse and a right angle would have an interior angle total of over $180^{\circ}$. That's not possible.
9. $x+67.25^{\circ}+2 x-15.8^{\circ}+x+10.15^{\circ}=180$ means $4 x=118.4$, so $x=29.6$. That means the angles measure $96.85^{\circ}, 43.4^{\circ}$, and $39.75^{\circ}$.
10. $x+2 x+68.4=180$ so $3 x=111.6$ and $x=37.2$. That means the angles measure $37.2^{\circ}$, $74.4^{\circ}$, and $68.4^{\circ}$.
11. Use $x$ as the measure of the second angle. Then $2 x+12.8+x+x-17.4=180$ so $4 x=184.6$ and $x=46.15$. The angles measure $105.1^{\circ}, 46.15^{\circ}$, and $28.75^{\circ}$.
12. (a) Sometimes true
(b) Never true
(c) Always true
(d) Sometimes true
(e) Sometimes true
(f) Never true
