1. [12 pts] If point $C=(-3,5)$ and point $D=(1,0)$, find the coordinates of a point $E$ so that $\overleftrightarrow{D C} \perp \overleftrightarrow{D E}$ and $D E=2 D C$. Show clear work.

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2. [12 pts] Given points $L=(0,3), M=(-1,-5)$, and $N=(2,-1)$, find the coordinates of a point $K$ so that $K, L, M$, and $N$ are the vertices of a trapezoid. Show clear work.

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3. [10 pts] Each set of descriptions below refers to triangles $\triangle C A T$ and $\triangle D O G$. Determine whether the given information guarantees that the triangles are congruent, then write the acronym involved and report the congruence using correct notation. DO NOT EXPLAIN FURTHER. If the given information does not guarantee congruence, say so.
(a) $C A=5, C T=4, D O=5, D G=4, \angle A \cong \angle O$
(b) $C A=5, D O=5, \angle A \cong \angle O, \angle C \cong \angle D$
(c) $C A=5, A T=5, C T=4, D O=5, D G=4, O G=5$
4. [16 pts - 8 each] In each diagram, apply the given information to find a pair of congruent triangles. Use correct notation to tell which two triangles they are and specify the acronym you use, then thoroughly explain how you arrived at your conclusion.
(a) Assume only that segments $\overline{F B}$ and $\overline{E C}$ are parallel and congruent to each other.

(b) Assume only that $B$ is the midpoint of $\overline{A C}$, that $\angle F B A \cong \angle D B C$, and that $\triangle F D B$ is equilateral.

5. [12 pts] A green figure and a blue figure are mathematically similar. The area of the green figure is $19.8 \mathrm{~cm}^{2}$, and the area of the blue figure is $120.5 \mathrm{~cm}^{2}$. If the blue figure is has a perimeter of 35.6 cm , what is the perimeter of the green figure, to the nearest tenth? Show clear work.
6. [12 pts] In the diagram, $\triangle P Q R \sim \triangle Q A B$. Also, $B Q=8, Q A=5, A B=8$, and $P R=25$. Find the length of $\overline{P B}$, to the nearest tenth. Show clear work.

7. (a) [4 pts] Complete the drawing so that a $90^{\circ}$ rotation around the marked point will demonstrate symmetry.

(b) [4 pts] Now complete the drawing so that lines $\ell$ and $m$ are lines of symmetry.

8. [8 pts - 4 each] Draw examples of the following.
(a) A figure that has $120^{\circ}$ rotational symmetry and also reflectional symmetry
(b) A figure that has translational symmetry but not reflectional symmetry
9. [6 pts - 2 each] Consider a pyramid with this base:

(a) How many axes of symmetry does the pyramid have?
(b) How many longitudinal planes of symmetry does the pyramid have?
(c) How many lateral planes of symmetry does the pyramid have?
10. (a) [2 pts] How many lateral axes of symmetry does a circular cylinder have?
(b) [2 pts] How many longitudinal axes of symmetry does a regular hexagonal prism have?
