

Math 131 - Dr. Miller - Activity #4: Negating Quantified Statements - Fall 2024

Negate each statement below, answering formally or informally to match the original statement. AVOID words like “none” and “no;” rephrase to use all/every instead.

1. All real numbers have squares larger than 3.

2. At least one perfect cube number is prime.

3.  $2^n < 0$  for some integer  $n$ .

4. For every pair of real numbers  $x$  and  $y$ ,  $x^2 + y^2 = 1$ . (The “and” is grammatical, to make a pair. It’s NOT a logic “and.”)

5.  $\forall x \in \mathbf{Z}^+$ , if  $x$  is prime or  $x < 2$ , then  $x$  isn’t even.

6.  $\exists x, y \in \mathbf{R}$  such that  $x > y$  but  $x^2 < y^2$ .