Write in standard form all possible Hindu-Arabic numerals that satisfy each set of clues below:

- 1. (a) There are no digits in the  $10^5$  position or higher. The thousands digit is an 8.
  - (b) The digit in the  $10^2$  position is twice that in the ten thousands position.
  - (c) The digit in the hundreds position equals that in the thousands position.
  - (d) In expanded form, the number shows  $3 \cdot 10^0$ .
  - (e) The digit in the tens position is two more that than in the ones position.
- 2. (a) There are no digits in the millions period or higher.
  - (b) The digit in the  $10^5$  position equals that in the thousands position.
  - (c) In expanded form, the number shows  $0 \cdot 10,000$ .
  - (d) The sum of the digits in the thousands period is 6.
  - (e) The digits in the ones period are either ones or zeros.
  - (f) There are only two even digits (0 IS even).
- 3. (a) There are no digits in the trillions period or higher.
  - (b) The billions period has only one non-zero digit; the millions period contains only 0s.
  - (c) The digit in the  $10^{10}$  position is 8.
  - (d) The thousands period contains all the same digit.
  - (e) The digit in the  $10^4$  position equals that in the  $10^0$  position.
  - (f) The digit in the hundreds place is 8 more than the digit in the ones place.
  - (g) In expanded form, the number shows the term  $3 \times 10$ .
- 4. (a) There are no digits in the millions period or higher.
  - (b) All of the digits are different; four of them are even.
  - (c) The digit in the  $10^3$  position is one more than that in the hundred thousands position.
  - (d) The digits in the tens and thousands position are 5 and 6 in some order.
  - (e) The digit in the  $10^2$  position is 4 times that in the  $10^0$  position.
- 5. (a) There are no digits in the ten billions position or higher.
  - (b) The numeral contains exactly eight 0s.
  - (c) The digits in the thousands period are all equal.
  - (d) The digit in the  $10^9$  position is less than 3.
  - (e) In expanded notation, the number shows  $8 \times 10,000,000$ .
- 6. (a) The numeral has no digits in the millions period or higher.
  - (b) The digits in the tens and  $10^4$  positions are equal, and even.
  - (c) The ones period and thousands period use the same digits, but not necessarily in the same order.
  - (d) The digit in the thousands place is 5 more than that in the ten thousands.
  - (e) The sum of the digits in the  $10^0$  position and the tens position is 3.
- 7. (a) The numeral has only three odd digits; one of them is in the  $10^7$  position.
  - (b) There are no odd digits in the ones period.
  - (c) Beginning with the ten thousands digit, the digits count in order up to 9 as one reads right to left.
  - (d) The digit 6 appears four times, but not in the  $10^1$  position.
  - (e) No other digit is repeated besides the 6.
  - (f) The digit in the  $10^3$  position equals that in the millions position.

- 8. (a) No digits are repeated except for zeros.
  - (b) The numeral shows the digits "002," uninterrupted and in that order.
  - (c) The highest position used is the one immediately to the left of the position with a 3 in it.
  - (d) The digit in the ten thousands position is 3 times that in the ones position.
  - (e) The digit in the  $10^3$  position is 3 less than that in the ten thousands position.
  - (f) The digits add up to 11.
- 9. (a) The digit in the  $10^0$  position equals that in the highest position used.
  - (b) The sum of the digits in the millions period is 3, but no ones appear in the period.
  - (c) There are no digits in the  $10^9$  position or higher.
  - (d) The numeral has four 1s in it.
  - (e) The digit in the hundred thousands place is the sum of the ones digit and the digit in the  $10^6$  place.
- 10. (a) Every digit is used exactly once, except for 7 and 3, which are not used at all.
  - (b) The digit in the highest position is odd.
  - (c) The digit in the thousands position is one more than that in the  $10^7$  position.
  - (d) Beginning with the  $10^2$  position, the digits count down in order (i.e., consecutively) as you read left to right.
  - (e) The ten thousands digit is even; the digit 9 is adjacent to the digit 1.

- 1. 48,853
- $2. \ 303,011 \quad or \quad 303,101 \quad or \quad 303,110$
- $3. \ 80,000,000,830 \qquad or \qquad 80,000,111,931$
- $4. 50,710,710 \quad or \quad 50,810,810 \quad or \quad 50,910,910$
- $5. 415, 862 \quad or \quad 435, 862 \quad or \quad 475, 862 \quad or \quad 495, 862$
- $6. 2,080,000,000 \quad or \quad 1,080,000,000$
- 7. 127, 721 or 305, 503
- $8. \ 9876546606 \ or \ 9876546626$
- 9. 63002 or 530021
- $10. \ 300311113 \ or \ 30311113 \ or \ 3611113$
- $11. \ 19802654 \ or \ 19082654$