

## Math 210 - Dr. Miller - Homework #32: Egyptian Numerals

Note: Due to typesetting difficulties, the following symbols are substituted in print:

@ is the scroll,  $\ddot{\Upsilon}$  is the lotus flower, < is the pointing finger,  $\propto$  is the tadpole, and &! is the astonished man.

You should, however, try to draw the symbols as we see them in our textbook.

1. Convert to Hindu-Arabic:

- (a)  $\ddot{\Upsilon}\ddot{\Upsilon} \cap//@\cap @$
- (b)  $\&! \&! \propto @@@@@\cap$
- (c)  $\langle\langle\cap\cap\cap\cap\cap\cap\cap@\cap//$

2. Convert to Egyptian:

- (a) 3,923
- (b) 250,506
- (c) 1,403,456

3. Give the Egyptian numeral that immediately follows the given one:

- (a)  $\ddot{\Upsilon}\ddot{\Upsilon}\propto // /$
- (b)  $@@// / / / / /$
- (c)  $\&! \cap$
- (d)  $\langle\langle\cap\cap\cap\cap\cap\cap\cap@\cap//$

4. Give the Egyptian numeral that immediately precedes the given one:

- (a)  $\&! \cap \cap$
- (b)  $\propto \langle \cap //$
- (c)  $\langle\langle\cap\cap\cap\cap\cap\cap\cap@\cap//$
- (d)  $@$

5. (a) Counting by tens, give the Egyptian numeral that immediately follows each numeral in Problems #3 and #4.  
(b) Counting by tens, give the Egyptian numeral that immediately precedes each numeral in Problems #3 and #4.  
(c) Counting by thousands, give the Egyptian numeral that immediately follows each numeral in Problems #3 and #4.  
(d) Counting by thousands, give the Egyptian numeral that immediately precedes each numeral in Problems #3 and #4, if possible. If not possible, say so.

6. Add entirely in Egyptian, showing all regroupings:

- (a)  $\propto\propto \langle\langle\langle \cap\cap\cap\cap\cap\cap\cap\cap // /$  and  $\langle\langle\langle\langle\langle \ddot{\Upsilon} \cap\cap\cap\cap\cap\cap\cap\cap // /$
- (b)  $\&! \propto\propto @@@@@\cap // / / / /$  and  $\propto \langle\ddot{\Upsilon} @@@@@\cap\cap // / /$
- (c)  $\&! \&! \langle\langle\langle @\cap\cap\cap\cap\cap\cap // /$  and  $\propto\propto \langle @@@@@ @@@@ @\cap\cap\cap\cap\cap\cap\cap // / /$

7. Subtract entirely in Egyptian, showing all regroupings:

- (a)  $\propto\propto @@@\cap\cap\cap\cap\cap\cap\cap\cap // / / /$  from  $\propto\propto\propto @@@@@\cap\cap\cap\cap\cap\cap\cap\cap // / /$
- (b)  $\langle\langle\langle \ddot{\Upsilon}\ddot{\Upsilon}\ddot{\Upsilon}\ddot{\Upsilon}\ddot{\Upsilon}\ddot{\Upsilon} \cap\cap /$  from  $\propto \ddot{\Upsilon}\ddot{\Upsilon}\ddot{\Upsilon}\ddot{\Upsilon}\ddot{\Upsilon}\ddot{\Upsilon}\ddot{\Upsilon} @ // / /$
- (c)  $\propto\propto \langle @@@@ @@@@ @\cap\cap\cap\cap\cap\cap\cap\cap // / / /$  from  $\&! \&! \langle\langle\langle @\cap\cap\cap\cap\cap\cap\cap\cap // / /$

1. (a) 2222

(b) 2,100,510

(c) 30,272

2. (a)  $\begin{array}{c} \heartsuit \\ \heartsuit \\ \heartsuit \end{array}$  @@@@ @@@@ @@@@  $\cap \cap \diagup \diagup$

(b)  $\infty \infty \langle \langle \langle \langle @@@@ @@@@ \diagup \diagup \diagup \diagup$

(c) &!  $\infty \infty \infty \begin{array}{c} \heartsuit \\ \heartsuit \\ \heartsuit \end{array}$  @@@@  $\cap \cap \cap \cap \cap \cap \diagup \diagup \diagup \diagup$

3. (a)  $\begin{array}{c} \heartsuit \\ \heartsuit \end{array}$   $\infty$   $\diagup \diagup \diagup$

(b) @ @  $\cap$

(c) &!  $\cap$  /

(d)  $\langle \langle \langle \cap \cap \cap \cap \cap \cap \cap \cap @ @ \diagup \diagup$

4. (a) &!  $\cap \diagup \diagup \diagup \diagup \diagup \diagup$

(b)  $\infty \langle \langle$  /

(c)  $\langle \langle \langle \cap \cap \cap \cap \cap \cap \cap \cap @ @ /$

(d)  $\cap \cap \diagup \diagup \diagup \diagup \diagup \diagup$

5. (no answers available)

6. (a)

$$\begin{array}{ccccccc}
 & (\infty) & & (@) & & & \\
 & \infty & \langle \langle \langle & & \cap \cap \cap \cap \cap \cap & \diagup \diagup \diagup \\
 plus & \langle \langle \langle \langle \langle & \begin{array}{c} \heartsuit \\ \heartsuit \end{array} & & \cap \cap \cap \cap \cap \cap & // \\
 & & & & & & //
 \end{array}$$

$$\text{equals } \infty \infty \infty \quad \begin{array}{c} \heartsuit \\ \heartsuit \end{array} \quad @ \quad \cap \cap \cap \cap \cap \cap \quad \diagup \diagup \diagup$$

(b)

$$\begin{array}{ccccccc}
 & (\infty) & & (@) & & & \\
 & \infty & \langle \langle \langle & \begin{array}{c} \heartsuit \\ \heartsuit \end{array} & @ @ @ @ @ @ & (\cap) & \\
 & & & & @ @ @ @ & \cap & \diagup \diagup \diagup \diagup \diagup \diagup \\
 & & & & & \cap & // \\
 plus & & \infty & \langle & \begin{array}{c} \heartsuit \\ \heartsuit \end{array} & @ @ @ @ & \cap \cap \quad // \\
 & & & & & & \cap \cap \quad // \\
 & & & & & & //
 \end{array}$$

$$\text{equals } \&! \infty \infty \infty \langle \begin{array}{c} \heartsuit \\ \heartsuit \end{array} \quad @ \quad \cap \cap \cap \cap \quad \diagup \diagup \diagup$$

(c)

$$\begin{array}{ccccccc}
 & (\infty) & & (@) & & & \\
 & \infty & \langle \langle \langle \langle & \begin{array}{c} \heartsuit \\ \heartsuit \end{array} & @ @ @ @ @ @ & \cap \cap \cap \cap \cap \cap & // \\
 plus & & & & @ @ @ @ @ @ & \cap \cap \cap \cap \cap \cap & // \\
 & & & & & & //
 \end{array}$$

$$\text{equals } \&! \&! \infty \langle \langle \langle \langle \langle \begin{array}{c} \heartsuit \\ \heartsuit \end{array} \quad @ \quad \cap \cap \cap \quad \diagup \diagup \diagup$$

7. (a)

$$\begin{array}{ccccccc}
 & & & & (n\cap n\cap n) & (/////) \\
 & & & & (\cap\cap\cap\cap\cap) & (/////) \\
 & & \alpha\alpha\alpha & @@@@ @ & \cap\wedge & // \\
 minus & \alpha\alpha & @@@ @@@ \cap\cap\cap\cap\cap\cap\cap & & & //// \\
 & & & & & & \\
 equals & \alpha & @ & & \cap\cap & //////////////
 \end{array}$$

(b)

$$\begin{array}{ccccccc}
 & & & & (n\cap n\cap n) & (/////) \\
 & & & & (\cap\cap\cap\cap\cap) & (/////) \\
 & & & & & & \\
 & & \langle\langle\langle & \overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}} & @ & // \\
 & & \cancel{\langle} & \overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}} & & \\
 minus & \langle\langle\langle & \overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}} & & \cap\cap & / \\
 & & & & & & \\
 equals & \langle\langle\langle\langle & \overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}} & & \cap\cap\cap\cap\cap\cap & // \\
 \end{array}$$

(c)

$$\begin{array}{ccccccc}
 & & & & (@@@@ @) & (n\cap n\cap n) & (/////) \\
 & & & & (@@@@ @) & (\cap\cap\cap\cap\cap) & (/////) \\
 & & (\alpha\alpha\alpha\alpha\alpha) & (\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}) & (@@@@ @) & (@@@@ @) & (/////) \\
 & & (\alpha\alpha\alpha\alpha\alpha) & (\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\cancel{\text{Y}}) & (@@@@ @) & (\cap\cap\cap\cap\cap\wedge) & (/////) \\
 & & \cancel{\&} \cancel{\&} & \langle\langle\langle \cancel{\wedge} & @ & \cap\cap\cap\cap\cap\cap & // \\
 & & \alpha\alpha & \cancel{\langle} & @@@@ @@@@ @ & \cap\cap\cap\cap\cap\cap & //// \\
 & & & & & & \\
 = & \& \& \alpha\alpha\alpha\alpha & \langle & \overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}} & @ & \cap\cap\cap & // \\
 & & & \alpha\alpha\alpha\alpha & \cancel{\langle} & \overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}}\overset{\heartsuit}{\text{Y}} & & \cap\cap\cap & // \\
 \end{array}$$