

In our course, a proof “launch” is the start of a proof up to one meaningful sentence beyond the NTS. I have given several PARTIAL launches below (I am purposely leaving out the NTS or other info sometimes). For each, tell which proof style is being attempted. It’s possible that a launch is NOT correct for any style, in which case, just write “NONE.”

1. Prop. - Suppose  $a$ ,  $b$ , and  $c$  are integers. If  $a$  divides  $b$  or  $a$  divides  $c$ , then  $a$  divides  $b + c$ .

“Proof.” Suppose  $a$ ,  $b$ , and  $c$  are integers.  
Suppose  $a$  divides  $b$  or  $a$  divides  $c$ .  
(NTS: ???)  
Assume  $a$  divides  $b$ . ...

2. Prop. - Suppose  $a$ ,  $b$ , and  $c$  are integers. If  $a$  divides  $b + c$ , then  $a$  divides  $b$  or  $a$  divides  $c$ .

“Proof.” Suppose  $a$ ,  $b$ , and  $c$  are integers.  
Suppose  $a$  divides  $b + c$  and  $a$  doesn’t divide  $c$ .  
(NTS: ???)  
Then for some integer  $q$ ,  $b + c = aq$ . ...

3. Suppose  $a$ ,  $b$ , and  $c$  are integers. If  $a$  divides both  $b$  and  $c$ , then  $a$  divides  $b + c$ .

“Proof.” Suppose  $a$ ,  $b$ , and  $c$  are integers.  
Assume that  $a$  does not divide  $b + c$ .  
(NTS: ???)  
Then  $ak \neq b + c$  for any integer  $k$ . ...

4. Prop. - Suppose  $m$  is an integer. If  $m^2$  is odd, then  $m$  is odd.

“Proof.” Suppose  $m$  is an integer.  
Assume  $m$  is odd.  
(NTS: if  $m^2$  is odd, then  $m$  is odd. )  
Then  $m = 2k + 1$  for some integer  $k$ . ...

5. Prop. - Suppose  $m$  is an integer. If  $m^2$  is odd, then  $m$  is odd.

“Proof.” Suppose  $m$  is an integer.  
Assume  $m$  is even.  
(NTS: ???)  
The  $m = 2k$  for some integer  $k$ . ...