

Prepare by studying the topics below, in conjunction with your notes, text/readings, handouts, Discussion/Participation, and graded and ungraded HW problems. You will be more successful if you strive to master the concepts in general, rather than simply memorizing specific examples that we have already done. Studying together is a plus.

Skills from Exam #1-2 and Discrete Math are still needed throughout the course. These include:

1. Identify hypothesis, conclusion in a conditional statement that's written using: if-then, trailing if, only if.
2. Write contrapositives. Recognize "if" versus "only if" directions in biconditional statements.
3. Negate: conditional, and, or, for all/each/every/any, there exists/is, at least one, greater/less/equal, etc.
4. Translate between conditional and universal statements as you find useful.
5. Be familiar with the notations \mathbf{Z} , \mathbf{Z}^+ , \mathbf{Z}^- , $\mathbf{Z}^+ \cup \{0\}$, similar variations for \mathbf{Q} and \mathbf{R} .
6. Use FORMAL definitions/statements: rational, even, odd, Division Algorithm, divides, FTA, intervals.
7. Know synonyms for divides (factor, multiple, divisor, divisible by) and how remainders work.

Non-Proof Tasks: Remember that formal statements/definitions have hypotheses. Don't forget to write them!

1. Formally define: domain, range, relation, reflexive, symmetric, transitive, function, onto, one-to-one.
2. Find elements related/not related to each other for a given relation, including:
 - (a) Domain or codomain are sets of numbers, power sets, Cartesian products.
3. Analyze statements as best fitting defn of function/not, one-to-one/not, onto/not.
4. Identify given formulas/verbal descriptions as function/not, one-to-one/not, onto/not as in HW #10.
5. Functions and relations may be defined using any of these earlier or familiar concepts:
 - (a) Parity, rationality, remainders, divisibility, other numeric concepts we've used in this class
 - (b) Intersection, union, set difference, cardinality, subsetness, other set concepts we've used in this class
 - (c) Algebra/pre-calc: equation/inequality solving, equations of lines/circles, functions, factoring, etc.
 - (d) Math terms and concepts from childhood courses or settings: fractions, decimals, geometry, etc.
6. Remember these closure axioms:
 - (a) \mathbf{Z} is closed under $+$, $-$, \times , and also non-negative exponentiation.
 - (b) \mathbf{R}^+ is closed under $+$, \times , \div , while \mathbf{R} is closed under $+$, $-$, \times , non-zero \div .
 - (c) You must use the formal definition of \mathbf{Q} instead of assuming it is closed in any way.
7. State your choice of set vs statement version of the Principle of Mathematical Induction (PMI).

Partial Proof Tasks: "Launches" There may be fewer tasks like this than on earlier exams.

1. Show the START of a proof by giving 3 pieces of info: assumptions, NTS, and ONE additional sentence.
 - (a) I will specify whether you're to go one sentence beyond a first, second, or even third NTS.
2. Remembering all previous styles may be helpful, but I will NOT be forcing specific styles on this exam:
 - (a) Conditional statements: Direct (including cases), by contrapositive, or by "or conclusion" style.
 - (b) Any statement: by contradiction (so remember how to negate EVERYTHING)
 - (c) "For all" proofs, constructive "there exists" proofs
 - i. For the constructive proof, you don't need to know the exact candidate; you can just write "Consider t " LITERALLY as your assumption and then move to NTS.
 - (d) Subsetness, set equality, or not-a-subset proof
 - (e) The SEPARATE directions of a biconditional statement directly, by ctp, or by contradiction
3. Statements here may use unfamiliar settings, but don't panic - these are simply launches, not full proofs.
4. Statements will primarily focus on RST, onto, one-to-one. PMI will NOT be included here.

Full Proof Tasks: Write COMPLETE proofs about relations and functions; write PMI proofs.

1. Emphasis will be on proofs, disproofs of: reflexive, symmetric, transitive properties, of one-to-one, onto.

2. Your skills in earlier styles are still needed.
 - (a) You should still be able to navigate cases, including WLOG, “or conclusion” style, contrapositive, contradiction, “for all,” constructive “there exists,” and proofs of their negations.
3. Styles may end up mixed now, as in our RST, one-to-one, onto proofs and disproofs.
 - (a) We’ve also seen instances where a proof by cases has ONE case that leads to a contradiction.
4. Remember that your NTS line or use of definitions can help you continue when stuck.
5. In a constructive “there exists” proof, your candidate might be a concrete value, or it might be a formula.
6. Beware algebra mistakes. Remember that I like to give partial credit.
7. **PMI proofs will appear only on the take-home portion of the exam (1-2 proofs).**
8. Remember these proof components:
 - (a) You **MUST** write your explicit assumptions at the outset, including universal hypotheses.
 - (b) You **MUST** write a formal NTS claim; a “meaning” add-on is helpful but not required.
 - (c) You **MUST** be clear that you have proved what was asked, via the “exit move” sentence.
 - (d) Write in SENTENCES. Proofs are never just a string of equalities or algebraic expressions. Such things must appear in context with words telling what they represent/what you’re doing with them.
9. I give PARTIAL CREDIT if you have the framework correct for your proof, even if you can’t do anything past the NTS. So put on the “Thus” and “exit move” ending sentences even if you’re stuck on the middle.

General Advice:

1. There will be 3-4 full proofs on the exam, with several smaller tasks.
2. Given the 50-minute time constraint, you’ll find that some correct proofs require only a few sentences.
3. Some statements may be similar to examples you’ve already seen, but others will not be (else I’m only testing your ability to imitate, rather than actually create your own proof).
4. By their very nature, proof exams require creativity.
 - (a) When required to be creative under a time constraint, it’s natural to feel lost, rushed, or even blind-sided. Try not to panic, but keep working to show me as much of your skills as possible.
 - (b) I like to give partial credit, so include as many *meaningful* ideas as possible, even if you’re stuck.
 - (c) Putting the “exit move” and other final sentences on the end typically earns some credit, regardless of whether you have a hole in the middle of your proof.
 - (d) Again, practice *A LOT* (there are plenty of problems left in the text!), so that you feel comfortable choosing a proof type AND making some progress on any statement you’re asked to prove.
5. If you feel you can’t finish in time, **DON’T PANIC**. I often take completion time into account when determining whether an exam deserves a curve or a bonus.
6. **DO YOUR BEST** in the exam period, and let me worry about the time factor.
7. Always remember: I like to give partial credit.

**You will have the entire class period to take the exam. When you finish, you may hand it in and leave.
We’ll discuss a useful Due Date for the Take-Home portion as a class.**

Please sit only in the separated rows we used last exam.
(This enhances integrity and gives me better access to come answer your questions.)

Students with SRU-approved accommodations should speak with me and process ODS requests ASAP.
ODS should proctor your exam since our classroom and my schedule are not automatically free.

Make-up Policy:

1. Notify me immediately if you’ll miss the exam.
2. Documentation will be required: get a doctor’s note, accident report, newspaper notice, etc.
3. If I excuse your absence, the Exam #3 content on our cumulative Final Exam in December will also be your make-up exam.
4. (D2L will show an artificial 0 for any excused absence until the end of the course.)