

Prepare for the exam by reviewing your notes, homework, reading, and handouts.

**Non-Proof Tasks:**

1. Formally state these definitions, including necessary universal hypotheses:
  - (a) Union, intersection, set difference, complement, Cartesian product, power set
  - (b) Relation from  $A$  to  $B$ , relation on  $A$
  - (c) Reflexive, symmetric, transitive, anti-symmetric properties
2. Create digraphs or sets of ordered pairs that are/aren't: reflexive, symmetric, transitive, anti-symmetric.
  - (a) Prepare for combinations of these, such as "is reflexive but not symmetric."
  - (b) Be aware of how false hypotheses affect symmetry, anti-symmetry, transitivity.
  - (c) I may require or forbid specific ordered pairs/ $xRy$  relationships, such as " $3R5$ " or " $(1, 1) \notin R$ ".
3. Given a digraph, set of ordered pairs, or verbal description of a relation, identify:
  - (a) Whether it is reflexive, symmetric, transitive, anti-symmetric; explain informally.
  - (b) Whether it is an equivalence relation, a partial order (reflexivity required); explain informally.

**Proof Tasks:** (Some are "rehearsed" proofs: we did them in class, so just rehearse your own write-up!)

1. Prove that something is/is not unique.
2. Prove that  $\emptyset \subseteq A$  for all sets  $A$ .
3. Prove my choice of direction in " $A \subseteq B$  iff  $\mathcal{P}(A) \subseteq \mathcal{P}(B)$ ".
  - (a) Pay close attention to the wording I give; points off for wrong direction.
  - (b) It may be helpful to review all the different variations (Exam #1) for stating a conditional.
4. Prove "subsetness," set equality, or "not a subset."
  - (a) Prepare for creative arithmetic, as in the  $1 - \frac{2+a}{b-7}$  or  $14x + 9y$  HW problems.
5. Prove set identities using chain-style proof, with only definitions and rules of logic.
6. Especially on set proofs, **precise** notation and math grammar will be required:
  - (a) Logic words join STATEMENTS while set operations join SETS - example: " $x \in A$  and  $B$ " is wrong; " $x \in A$  and  $x \in B$ " is right, as is " $x \in A \cap B$ ."
  - (b) We assume or show or conclude STATEMENTS, not SETS - example 1: "Assume  $A \times B$ " is wrong; "Assume  $(x, y) \in A \times B$ " is right.
  - (c) Example 2: "So  $A \cap B$ " is wrong; "So  $A \cap B = B$ " is correct, as is "So  $x \in A \cap B$ ."
7. Prove whether a given relation is/is not reflexive, symmetric, transitive, anti-symmetric.
8. Counterexamples should be rigorous: give your candidate, and show it meets all conditions.
  - (a) I will not OPENLY ask for counterexamples; that is, instructions won't say "Give a cex to the following statement ...."
  - (b) However, most of the "not" proof tasks listed above require the creation of a cex.
9. **Take-home problem:** Prove a result by PMI.