Math 310 - Dr. Miller - Homework \#17: Percent Reasoning and Basic Applications

1. Two quantities are described in each part below. Decide whether the first is larger than, smaller than, or equal to the second.
(a) A number, or $30 \%$ of that number
(b) A number, or $500 \%$ of that number
(c) $30 \%$ of a number, or 0.03 times the number
(d) 1.5 times a number, or $1.5 \%$ of the number
(e) A number plus $30 \%$ of itself, or $130 \%$ of the number
(f) A number minus $50 \%$ of itself, or $75 \%$ of the number
(g) $150 \%$ of a number, or 2 times the number
(h) $105 \%$ of a number, or 1.5 times the number
(i) $1.05 \%$ of a number, or the original number
(j) One third of a number, or $30 \%$ of a number
(k) $30 \%$ of $50 \%$ of a number, or $20 \%$ of the number
(l) $50 \%$ of $150 \%$ of a number, or the original number
(m) $40 \%$ of a number, or $20 \%$ of $20 \%$ of the number
2. (a) $x$ is $75 \%$ of a number. Is the number more or less than $x$ ?
(b) $y$ is $105 \%$ of a number. Is the number more or less than $y$ ?
(c) If $x$ is a positive number, is $x+1$ more or less than $100 \%$ of $x$ ?
(d) If you take $10 \%$ of $10 x$, how does the result compare to $x$ ?
(e) If you take $10 \%$ of $10+x$, how does the result compare to $x$ ?
3. Solve these non-contextual problems.
(a) What number is $18.3 \%$ of 50 ?
(b) What percent is 18.3 of 50 ?
(c) 13.8 is $50 \%$ of what number?
(d) $65 \%$ of 120 is what?
(e) 75 is what percent of 120 ?
(f) 65 is $18 \%$ of $x$. What is $x$ ?
4. Solve:
(a) Jodi had 180 candy bars at the start of trick-or-treating, and 35 were left at the end. Is this a percent increase or decrease, and by what percent (to the nearest tenth of a percent)?
(b) New homes in Outer County cost an average of $\$ 180,000$ in 2016 and $\$ 155,000$ in 2015. Is this a percent increase or decrease, and by what percent (to the nearest tenth of a percent)?
(c) Enrollment at Suburb Elementary School was 536 in 2019 and 589 in 2020. Is this a percent increase or decrease, and by what percent (to the nearest tenth of a percent)?
(d) Dianne used to have 1017 comics in her collection, and now she has 1306. Is this a percent increase or decrease, and by what percent (to the nearest tenth of a percent)?
5. (a) The number is larger than $30 \%$ of that number.
(b) The number is smaller than $500 \%$ of that number.
(c) $30 \%$ of a number is larger than 0.03 times the number. ( 0.03 times the number is only $3 \%$.)
(d) 1.5 times a number is larger than $1.5 \%$ of the number. ( 1.5 times the number is $150 \%$.)
(e) A number plus $30 \%$ of itself is equal to $130 \%$ of the number.
(f) A number minus $50 \%$ of itself is smaller than $75 \%$ of the number. (A number minus $50 \%$ of itself leaves only $50 \%$.)
(g) $150 \%$ of a number is smaller than 2 times the number. ( 2 times the number is $200 \%$.)
(h) $105 \%$ of a number is smaller than 1.5 times the number. ( 1.5 times the number is $150 \%$.)
(i) $1.05 \%$ of a number is smaller than the original number. (The original is $100 \%$, not $1 \%$.)
(j) One third of a number is larger than $30 \%$ of a number. (One third of a number is $33 \frac{1}{3} \%$.)
(k) $30 \%$ of $50 \%$ of a number is smaller than or $20 \%$ of the number. ( $30 \%$ of $50 \%$ is $0.3 \times 0.5=0.15=15 \%$.)
(l) $50 \%$ of $150 \%$ of a number is smaller than the original number. ( $50 \%$ of $150 \%$ is $0.5 \times 1.5=0.75=75 \%$ of the number.)
(m) $40 \%$ of a number is larger than $20 \%$ of $20 \%$ of the number. $(20 \%$ of $20 \%$ is $0.2 \times 0.2=$ $0.04=4 \%$.)
6. (a) The number is more than $x$.
(b) The number is less than $y$.
(c) $x+1$ is more than $100 \%$ of $x$.
(d) It equals $x$.
(e) It is probably less than $x$. (Unless $x$ is already a very tiny decimal...)
7. (a) 9.15
(b) $36.6 \%$
(c) 27.6
(d) 78
(e) $62.5 \%$
(f) $361 \frac{1}{9}$
8. (a) decrease, $80.6 \%$
(b) increase, $16.1 \%$
(c) increase, $9.9 \%$
(d) increase, $28.4 \%$
