

Math 310 - Dr. Miller - Homework #29: Dimension Analysis

1. Convert as indicated:

- (a) \$6.75 per hour to cents per minute
- (b) 12 cents per day to dollars per year
- (c) \$12 per square yard to cents per square inch
- (d) 65 miles per hour to feet per second
- (e) 3 watts per hour to kilowatts per week
- (f) 3 square meters per minute to square centimeters per second
- (g) 6 liters per second to kiloliters per hour
- (h) a fourth of a kilogram per day to grams per hour
- (i) 16 feet per second to meters per second ($2.54 \text{ cm} = 1 \text{ in}$)

2. Convert as indicated:

- (a) 2.5 foot-pounds to inch-ounces
- (b) 32 feet per second per second to kilometers per minute-squared
- (c) 25 man-hours to team-minutes, where 1 team equals 10 men/people
- (d) 6.5 kilowatt-hours to watt-seconds

1. (a) $\frac{\$6.75}{1 \text{ hour}} \times \frac{100 \text{ cents}}{\$1} \times \frac{1 \text{ hour}}{60 \text{ min}} = 11.3 \text{ cents per minute}$
 - (b) $\frac{12 \text{ cents}}{1 \text{ day}} \times \frac{365 \text{ days}}{1 \text{ year}} \times \frac{\$1}{100 \text{ cents}} = \43.80 per year
 - (c) $\frac{\$12}{1 \text{ yd} \cdot \text{yd}} \times \frac{100 \text{ cents}}{\$1} \times \frac{1 \text{ yd}}{36 \text{ in}} \times \frac{1 \text{ yd}}{36 \text{ in}} = 0.9 \text{ cents per square inch (not 90 cents!)}$
 - (d) $\frac{65 \text{ miles}}{1 \text{ hour}} \times \frac{5280 \text{ feet}}{1 \text{ mile}} \times \frac{1 \text{ hour}}{60 \text{ min}} \times \frac{1 \text{ min}}{60 \text{ sec}} = 95.3 \text{ feet per second}$
 - (e) $\frac{3 \text{ watts}}{1 \text{ hour}} \times \frac{1 \text{ kilowatt}}{1000 \text{ watts}} \times \frac{24 \text{ hours}}{1 \text{ day}} \times \frac{7 \text{ days}}{1 \text{ week}} = 0.5 \text{ kW per month}$
 - (f) $\frac{3 \text{ m} \cdot \text{m}}{1 \text{ min}} \times \frac{100 \text{ cm}}{1 \text{ m}} \times \frac{100 \text{ cm}}{1 \text{ m}} \times \frac{1 \text{ min}}{60 \text{ sec}} = 500 \text{ cm}^2 \text{ per second}$
 - (g) $\frac{6 \ell}{1 \text{ sec}} \times \frac{1 \text{ k}\ell}{1000 \ell} \times \frac{60 \text{ sec}}{1 \text{ min}} \times \frac{60 \text{ min}}{1 \text{ hour}} = 21.6 \text{ k}\ell \text{ per hour}$
 - (h) $\frac{0.25 \text{ kg}}{1 \text{ day}} \times \frac{1000 \text{ g}}{1 \text{ kg}} \times \frac{1 \text{ day}}{24 \text{ hours}} = 10.4 \text{ grams per hour}$
 - (i) $\frac{16 \text{ ft}}{1 \text{ sec}} \times \frac{12 \text{ in}}{1 \text{ ft}} \times \frac{2.54 \text{ cm}}{1 \text{ in}} \times \frac{1 \text{ m}}{100 \text{ cm}} = 4.9 \text{ meters per second}$
2. (a) $\frac{2.5 \text{ ft} \cdot \text{lb}}{1} \times \frac{12 \text{ in}}{1 \text{ ft}} \times \frac{16 \text{ oz}}{1 \text{ lb}} = 480 \text{ in} \cdot \text{oz}$
 - (b) $\frac{32 \text{ ft}}{\text{sec} \cdot \text{sec}} \times \frac{60 \text{ sec}}{1 \text{ min}} \times \frac{60 \text{ sec}}{1 \text{ min}} \times \frac{12 \text{ in}}{1 \text{ ft}} \times \frac{2.54 \text{ cm}}{1 \text{ in}} \times \frac{1 \text{ m}}{100 \text{ cm}} \times \frac{1 \text{ km}}{1000 \text{ m}} = 35.11 \text{ km per min}^2$
 - (c) $\frac{25 \text{ man} \cdot \text{hr}}{1} \times \frac{1 \text{ team}}{10 \text{ men}} \times \frac{60 \text{ min}}{1 \text{ hour}} = 150 \text{ team} \cdot \text{minutes}$
 - (d) $\frac{6.5 \text{ kW} \cdot \text{hr}}{1} \times \frac{1000 \text{ W}}{1 \text{ kW}} \times \frac{60 \text{ min}}{1 \text{ hr}} \times \frac{60 \text{ sec}}{1 \text{ min}} = 23,400,000 \text{ W} \cdot \text{sec}$